

CSC-343 ARTIFICIAL INTELLIGENCE
LECTURE 5.3
PROGRAMMING ASSIGNMENT 4

DATA:

emails = [(“Where to hide a dead body”, 1), (“Grateful dead body of work”, 0)]

MODEL: (Naïve Bayes)

$$P(\text{Spam} | \text{word1}, \text{word2}, \dots, \text{wordn}) = \alpha P(\text{Spam}) \prod P(\text{wordi} | \text{Spam})$$

CLASSIFIER:

$$P(\text{spam} | \text{word1}, \text{word2}, \dots, \text{wordn}) > P(\neg \text{spam} | \text{word1}, \text{word2}, \dots, \text{wordn})$$

B-BOW:

<i>email</i>	Where	To	Hide	A	Dead	Body	Grateful	Of	Work	Spam
1	1	1	1	1	1	1	0	0	0	True
2	0	0	0	0	1	1	1	1	1	False

PART 1 - PRIORS

$$P(\text{Spam} | \text{word1}, \text{word2}, \dots, \text{wordn}) = \alpha P(\text{Spam}) \prod P(\text{wordi} | \text{Spam})$$

$$P(\text{spam}) = \text{count}(\text{spam emails}) / \text{count}(\text{all emails})$$

$$P(\neg \text{spam}) = \text{count}(\text{ham emails}) / \text{count}(\text{all emails})$$

Spam	P(Spam)
True	p1
False	p2

PART 2 – JOINT PROBABILITIES

$$P(\text{Spam} | \text{word}_1, \text{word}_2, \dots, \text{word}_n) = \alpha P(\text{Spam}) \prod P(\text{word}_i | \text{Spam})$$

$$P(\text{word}_i | \text{Spam}) = P(\text{word}_i, \text{Spam}) / P(\text{Spam})$$

Joint Probabilities: $P(\text{word}_i, \text{Spam})$

jp1 = count(spam emails containing word_i) / count(all emails)

jp2 = count(spam emails NOT containing word_i) / count(all emails)

jp3 = count(ham emails containing word_i) / count(all emails)

jp4 = count(ham emails NOT containing word_i) / count(all emails)

word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)
T	T	jp1	T	T	jp1	T	T	jp1
F	T	jp2	F	T	jp2	F	T	jp2
T	F	jp3	T	F	jp3	T	F	jp3
F	F	jp4	F	F	jp4	F	F	jp4
word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)
T	T	jp1	T	T	jp1	T	T	jp1
F	T	jp2	F	T	jp2	F	T	jp2
T	F	jp3	T	F	jp3	T	F	jp3
F	F	jp4	F	F	jp4	F	F	jp4
word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)
T	T	jp1	T	T	jp1	T	T	jp1
F	T	jp2	F	T	jp2	F	T	jp2
T	F	jp3	T	F	jp3	T	F	jp3
F	F	jp4	F	F	jp4	F	F	jp4

PART 3 – CONDITIONAL PROBABILITIES

$$P(\text{Spam} | \text{word}_1, \text{word}_2, \dots, \text{word}_n) = \alpha P(\text{Spam}) \prod P(\text{word}_i | \text{Spam})$$

$$P(\text{word}_i | \text{Spam}) = P(\text{word}_i, \text{Spam}) / P(\text{Spam})$$

word _i	Spam	P(word _i Spam)	word _i	Spam	P(word _i Spam)	word _i	Spam	P(word _i Spam)
T	T	cp1	T	T	cp1	T	T	cp1
F	T	cp2	F	T	cp2	F	T	cp2
T	F	cp3	T	F	cp3	T	F	cp3
F	F	cp4	F	F	cp4	F	F	cp4

word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)	word _i	Spam	P(word _i , Spam)
T	T	cp1	T	T	cp1	T	T	cp1
F	T	cp2	F	T	cp2	F	T	cp2
T	F	cp3	T	F	cp3	T	F	cp3
F	F	cp4	F	F	cp4	F	F	cp4

word _i	Spam	P(word _i Spam)	word _i	Spam	P(word _i Spam)	word _i	Spam	P(word _i Spam)
T	T	cp1	T	T	cp1	T	T	cp1
F	T	cp2	F	T	cp2	F	T	cp2
T	F	cp3	T	F	cp3	T	F	cp3
F	F	cp4	F	F	cp4	F	F	cp4

PART 4 - CLASSIFICATION

email	$P(\text{spam} \text{email})$ = $P(\text{spam} \text{word}_1, \text{word}_2, \dots, \text{word}_n)$ = $P(\text{spam}) \prod P(\text{word}_i \text{spam})$ = $P(\text{spam}) \text{cp1}$	$P(\neg \text{spam} \text{email})$ = $P(\neg \text{spam} \text{word}_1, \text{word}_2, \dots, \text{word}_n)$ = $P(\neg \text{spam}) \prod P(\text{word}_i \neg \text{spam})$ = $P(\neg \text{spam}) \text{cp3}$	Our Prediction $P(\text{spam} \text{email}) > P(\neg \text{spam} \text{email})$	Data
1				True
2				False

PART 5 – ACCURACY

$$\text{Accuracy} = \text{Count}(\text{Our Prediction} == \text{Prediction from Data}) / \text{Count}(\text{Emails})$$